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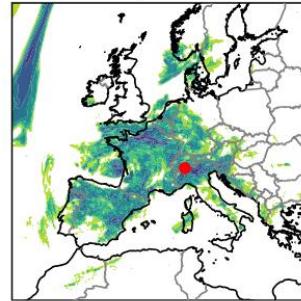
# Numerics of the 1D Richards Equation and implications for land surface modelling on the kilometer-scale

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Christoph Schär (ETHZ)



# Surface Runoff Formation in COSMO

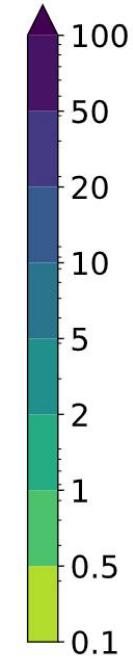
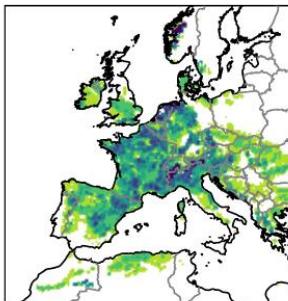
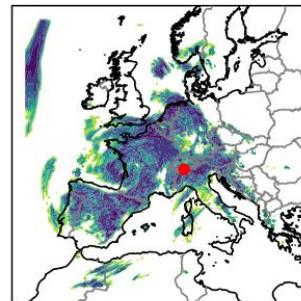
Precipitation



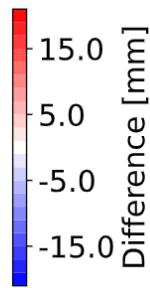
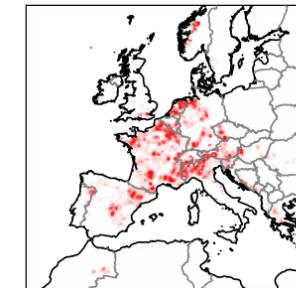
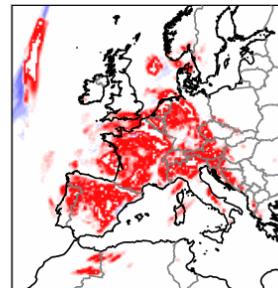
Surface Runoff



$\Delta x = 2.2 \text{ km, CRM}$



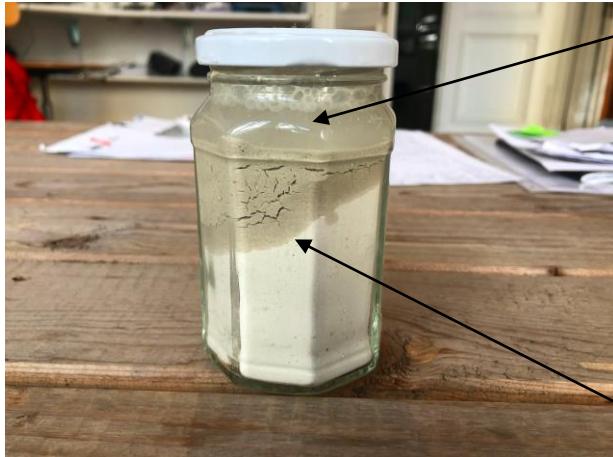
Difference





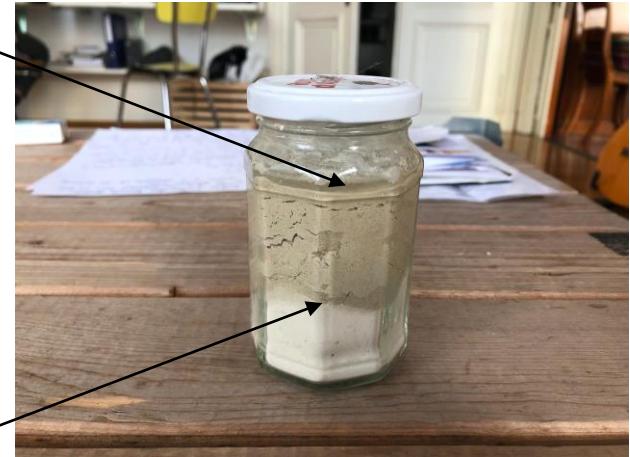
# Propagation of soil water

5 min



Ponding Water

1 hour



Wetting Front



# Mathematical Formulation

$$\frac{\partial \theta}{\partial t} = -\frac{\partial F}{\partial z} + I - Q - ET \quad \text{Mass Conservation}$$





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$$F = -D(\theta) \frac{\partial \theta}{\partial z} + K(\theta) \quad \text{Darcy's Law}$$

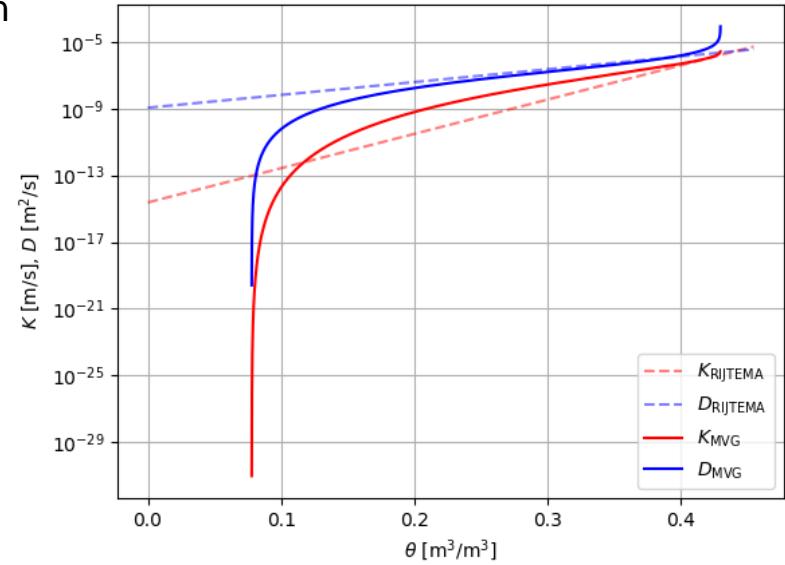


# Mathematical Formulation

$$\frac{\partial \theta}{\partial t} = -\frac{\partial F}{\partial z} + I - Q - ET \quad \text{Mass Conservation}$$

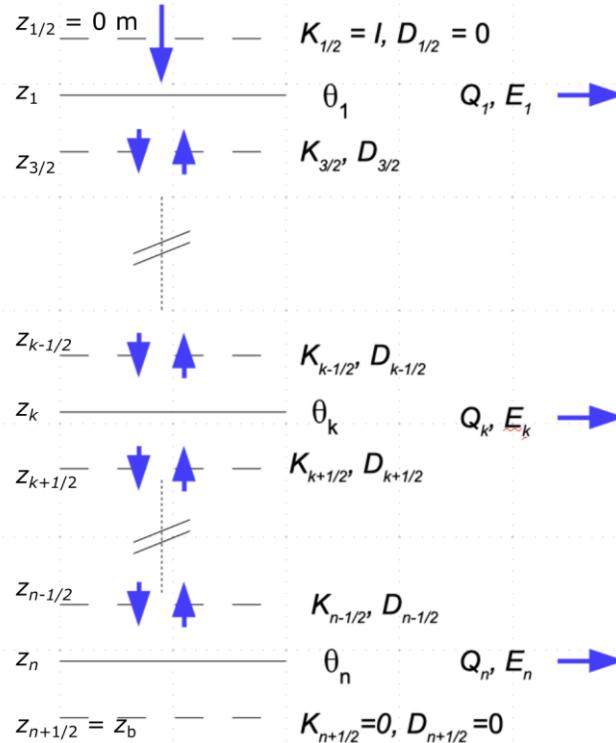
$$F = -D(\theta) \frac{\partial \theta}{\partial z} + K(\theta) \quad \text{Darcy's Law}$$

Assumptions on K, D from soil physics.  
E.g. Rijtema (1969) or Mualem –  
van Genuchten (1976, 1980)





# Numerical Implementation



Follows TERRA ML implementation.

Staggered Grid with fluxes on layer interfaces.

Zero flux bottom BC + Diagnosed Runoff Q  
(Schlemmer et al., 2018).

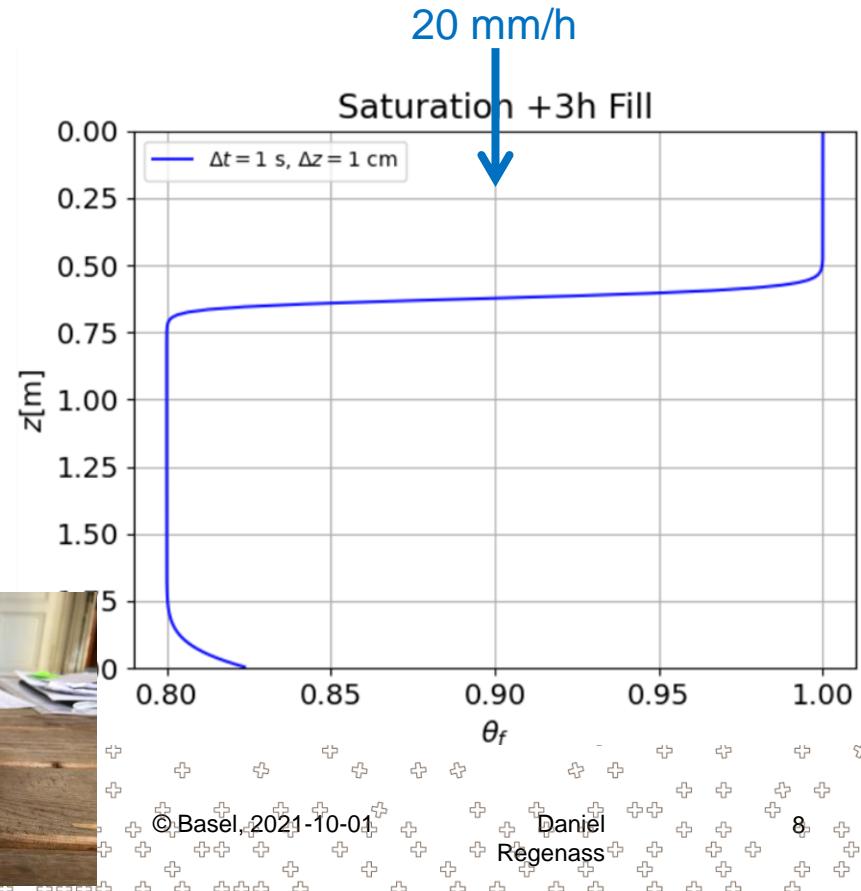
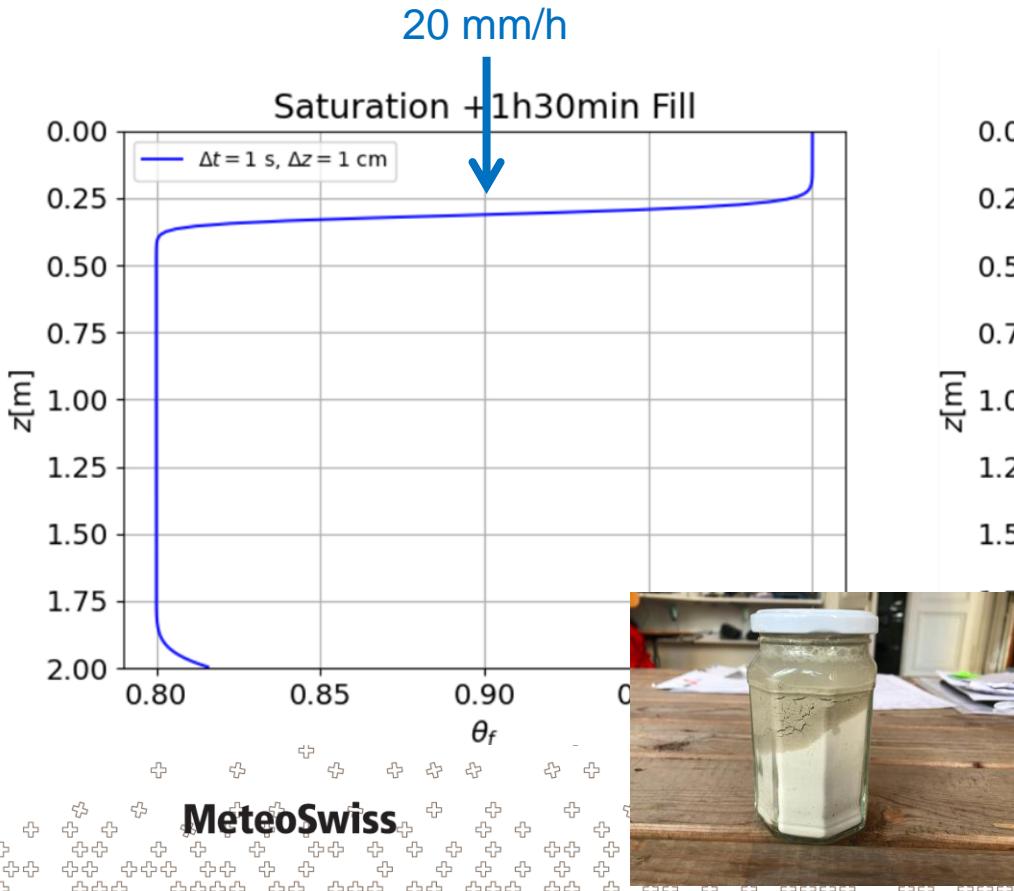
Hydraulic Diffusion treated implicitly.

Flux corrected transport for explicit part (Boris and Book, 1973; Zalesak, 1979; Schlemmer et al., 2018).

Available as Python Standalone.

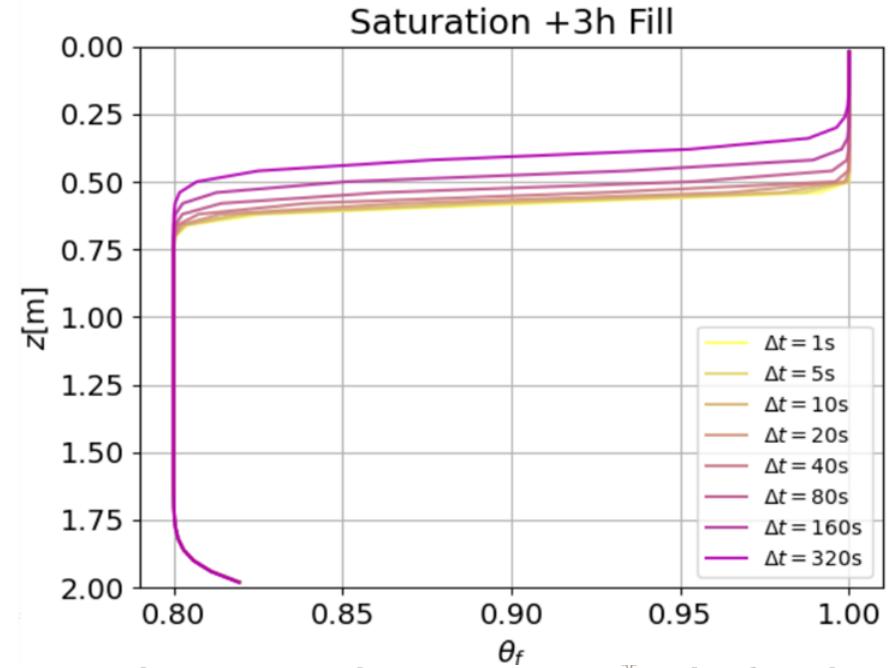
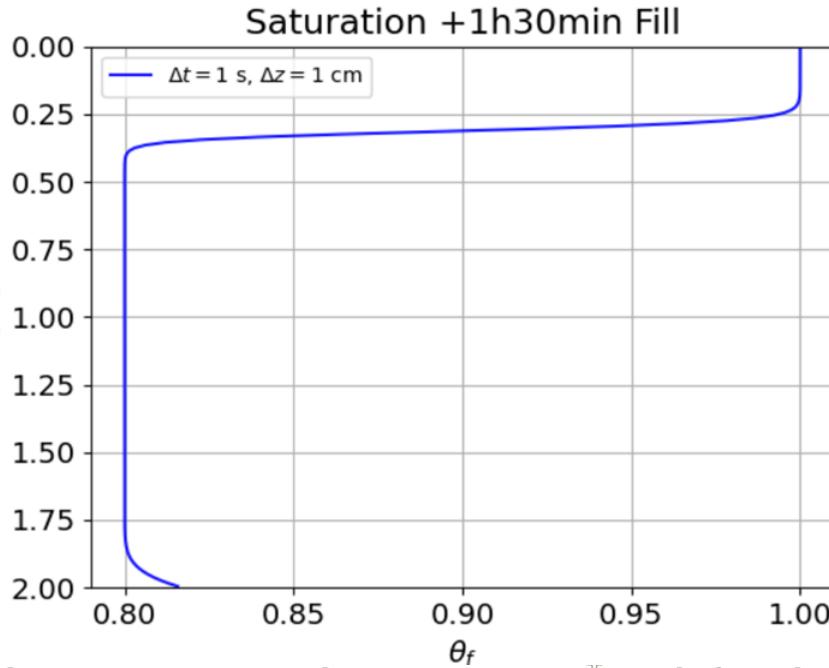


# Fill Experiment



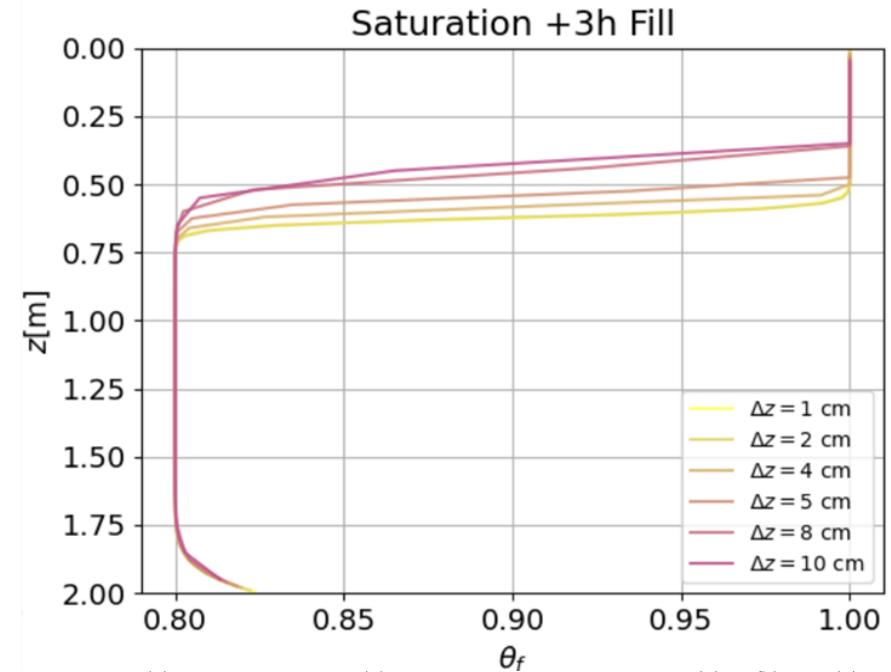
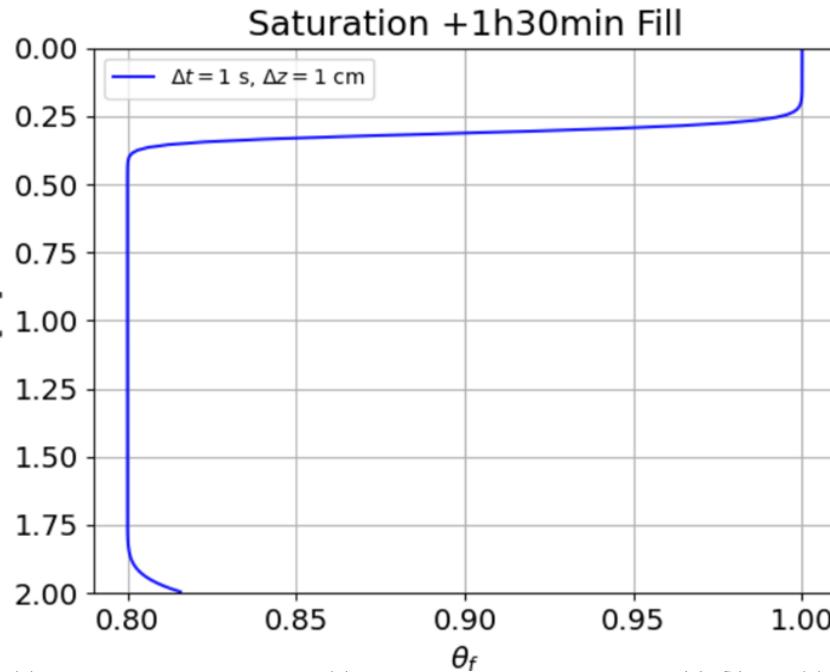


# Time Step Dependency



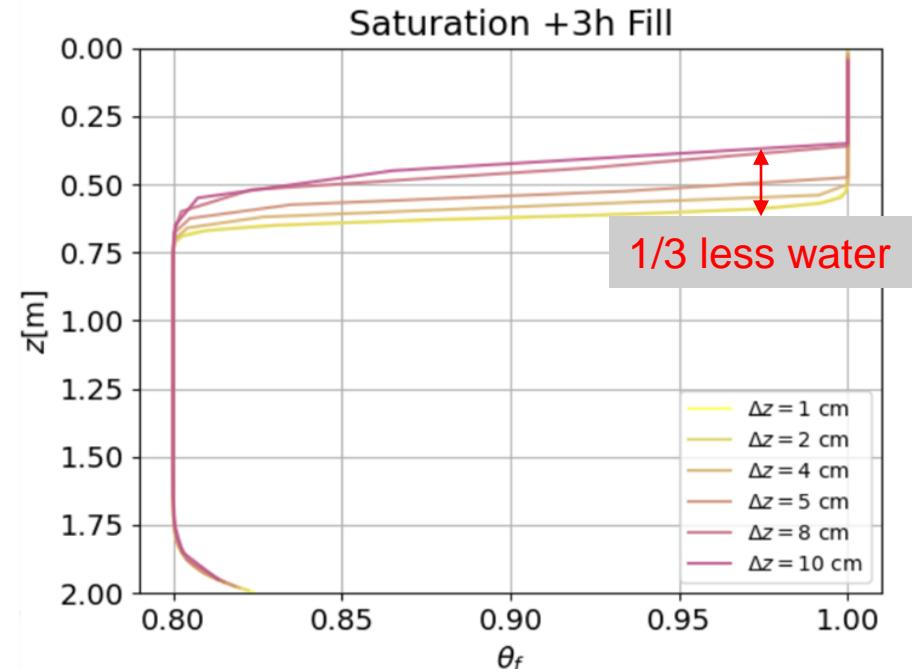
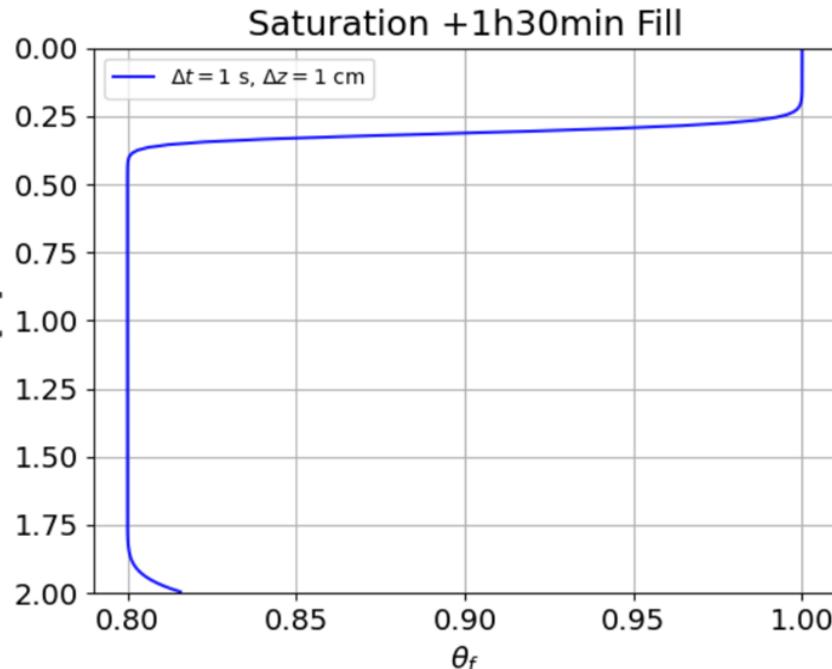


# Resolution Dependency



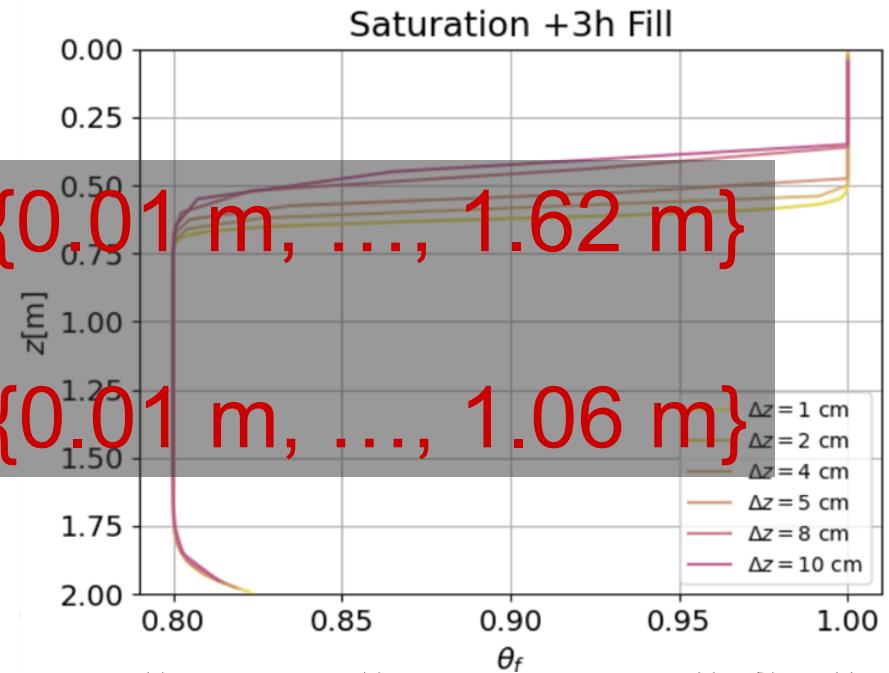
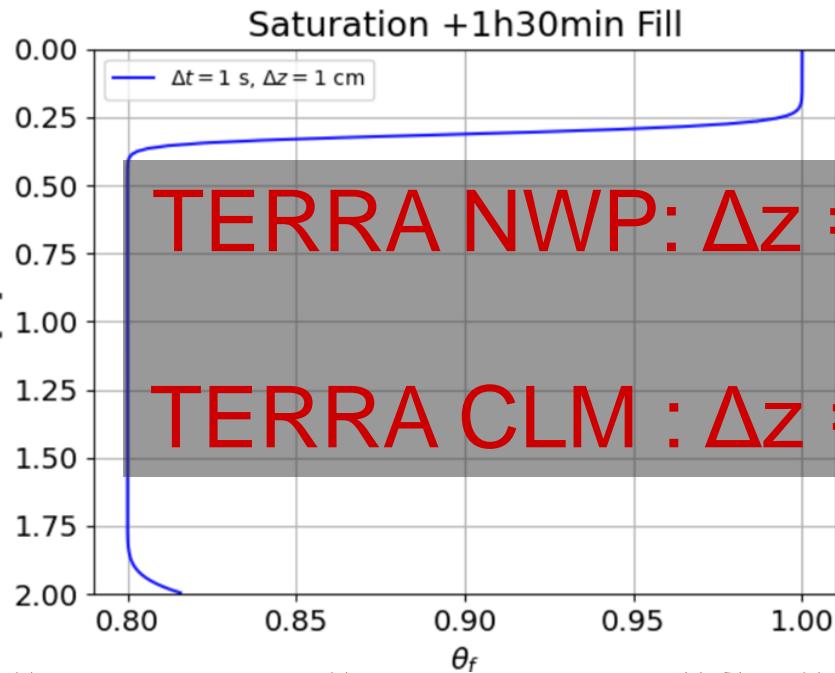


# Resolution Dependency





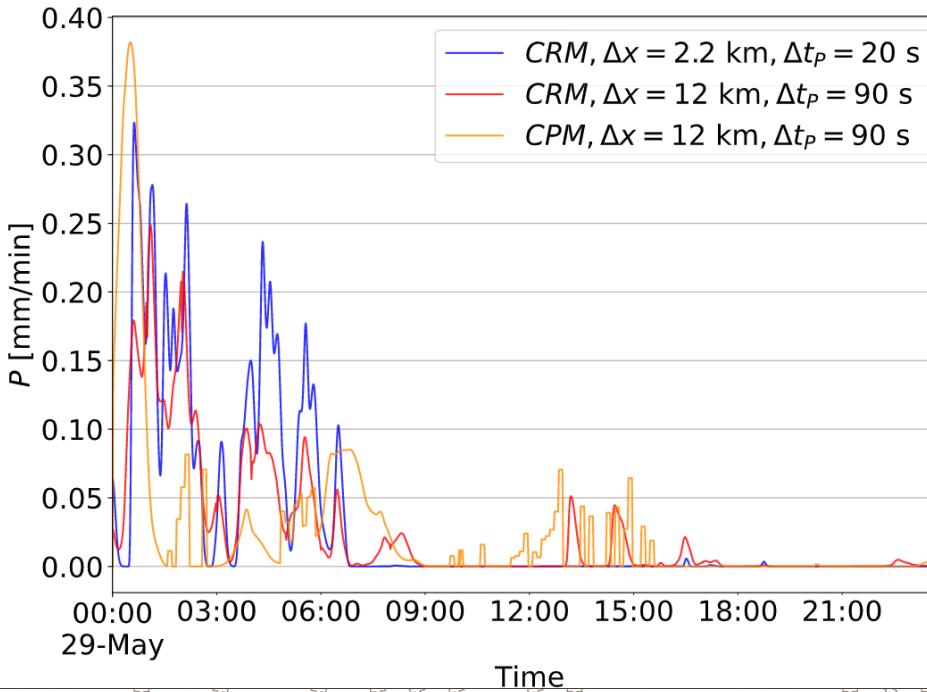
# Resolution Dependency





# 'Realistic' Precipitation Experiment

Precipitation Rates for Baceno and Pizzo Stagno.



Extracted from 24h forecast experiment

Precipitation output on time step level

Python standalone forced with precipitation time series.



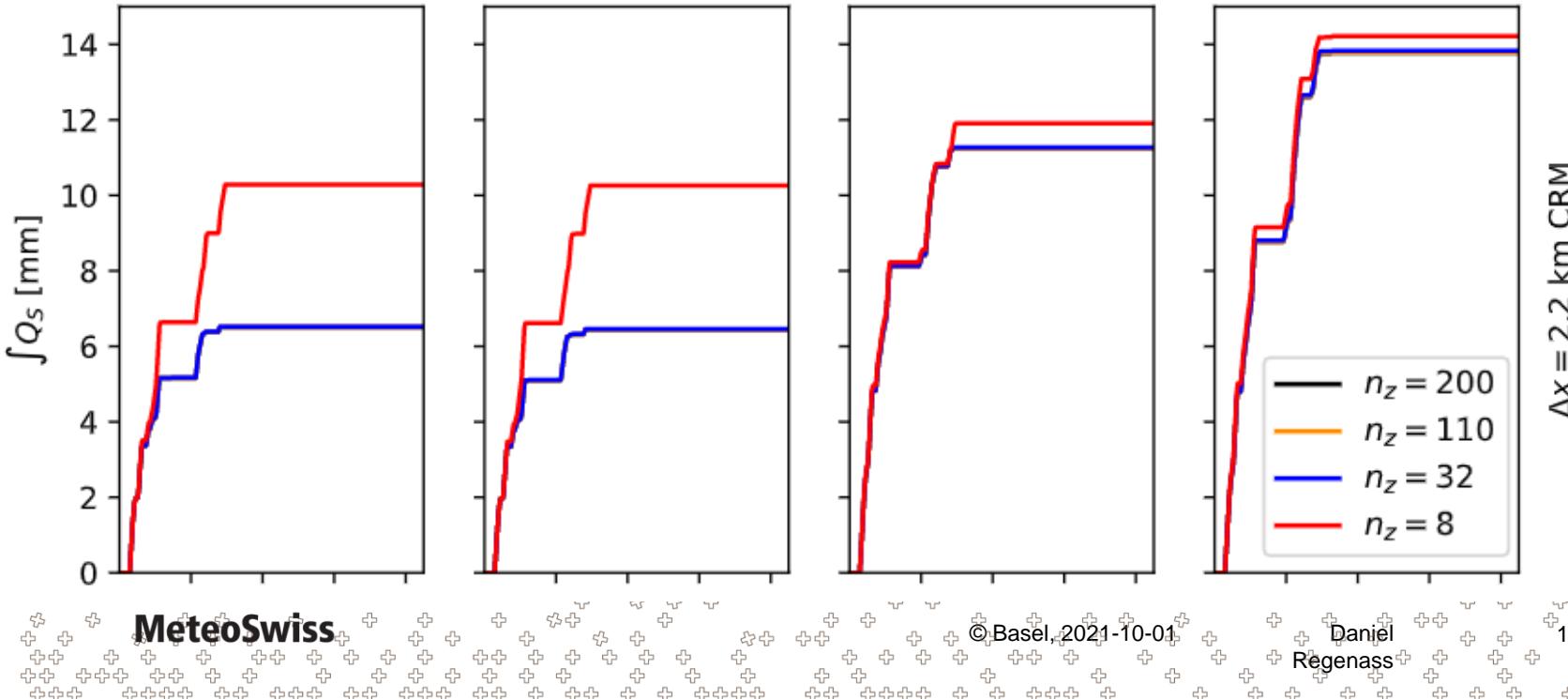
# Surface Runoff Formation

$\Delta t_r = 20\text{s}$ ,  
 $\Delta t = 20\text{s}$

$\Delta t_r = 90\text{s}$ ,  
 $\Delta t = 20\text{s}$

$\Delta t_r = 90\text{s}$ ,  
 $\Delta t = 90\text{s}$

$\Delta t_r = 180\text{s}$ ,  
 $\Delta t = 180\text{s}$





# Summary

- 1D Richards Equation is sensitive to vertical discretization and time stepping.
- Vertical resolution in many LSMs too coarse to achieve an adequate representation of the solution during the infiltration process
- Direct impact on water partitioning at the surface.





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