

# A 4DEnVar scheme for Arome-France : presentation and evaluation

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## Introduction

- At Météo-France, a 3DEnVar scheme, utilising OOPS, will become operational for AROME-France next month in the current 1hr data assimilation cycle (instead of the historical 3D-Var one) : see V. Vogt's talk at 45th EWGLAM and 30th SRNWP Meeting 2023
- The next evolution planned for the next E-suite : 4DEnVar in the 1hr cycle in order to :
  - assimilate 15min observations : radar, surface, ground GNSS and SEVIRI observations
  - improve the comparison to the background for the others ones (polar satellites, ...)
- the present talk aims :
  - to introduce the 4DEnVar scheme
  - to introduce the MF's AROME-France implementation
  - to show some evaluation results against 3DEnVar

# outlines

- **Introduction to a 4DEnVar DA system**
- **Proposal for the next AROME-France E-suite and evaluation.**

## Towards a 4D scheme

3D-Var/3DEnVar :  $J(\delta \mathbf{x}) = \frac{1}{2}(\delta \mathbf{x})^T \mathbf{B}^{-1}(\delta \mathbf{x}) + \frac{1}{2}(\mathbf{d} - \mathbf{H}\delta \mathbf{x})^T \mathbf{R}^{-1}(\mathbf{d} - \mathbf{H}\delta \mathbf{x})$

4D-Var :  $J(\delta \mathbf{x}) = \frac{1}{2}(\delta \mathbf{x})^T \mathbf{B}^{-1}(\delta \mathbf{x}) + \frac{1}{2} \sum_{i=0}^K (\mathbf{d}_i - \mathbf{H}_i \mathbf{M}_{0 \rightarrow i} \delta \mathbf{x})^T \mathbf{R}_i^{-1}(\mathbf{d}_i - \mathbf{H}_i \mathbf{M}_{0 \rightarrow i} \delta \mathbf{x})$

- a LAM 4D-var is available in IFS/ARP/ARO/HAR code but relies on the ALADIN model
  - direct model : hydrostatic dynamic, less sophisticated physic (only 4 hydrometeors without graupel), without surfex
  - Tangent and adjoint model : hydrostatic, very simple simplified physic

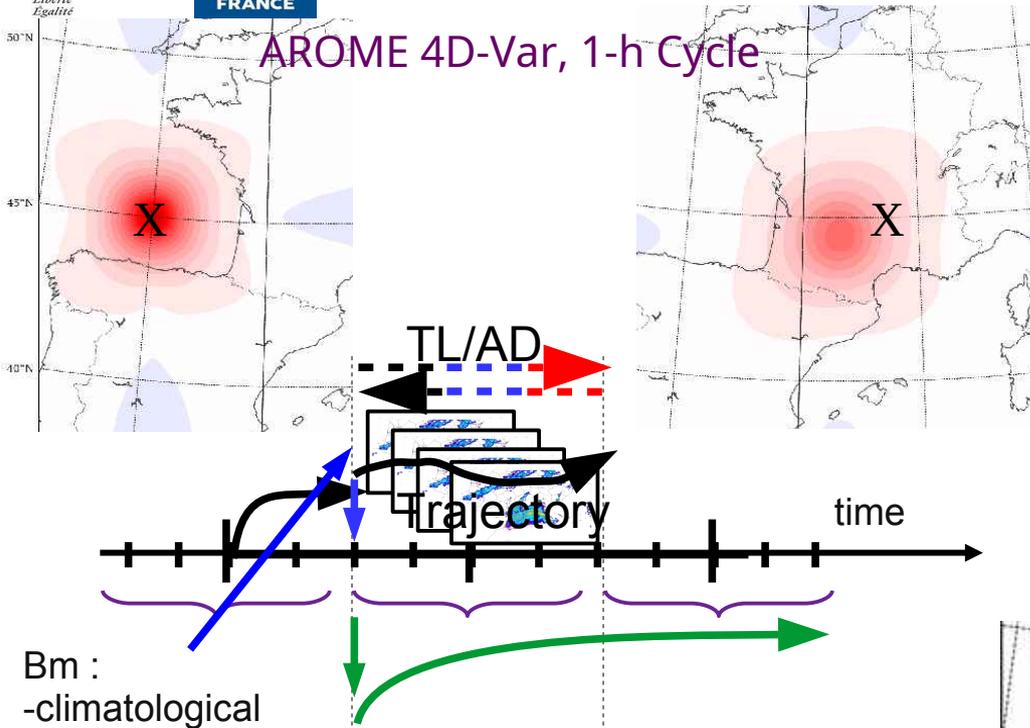
→ In a 4DEnVar scheme :

4DEnVar :  $J(\underline{\delta \mathbf{x}}) = \frac{1}{2}(\underline{\delta \mathbf{x}})^T \underline{\mathbf{B}}^{-1}(\underline{\delta \mathbf{x}}) + \frac{1}{2}(\underline{\mathbf{d}} - \underline{\mathbf{H}}\underline{\delta \mathbf{x}})^T \underline{\mathbf{R}}^{-1}(\underline{\mathbf{d}} - \underline{\mathbf{H}}\underline{\delta \mathbf{x}})$  (Desroziers et al. 2014)

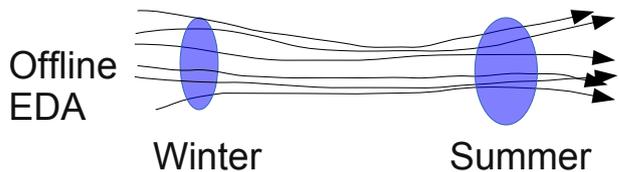
$$\underline{\delta \mathbf{x}} = \begin{pmatrix} \delta \mathbf{x}_0 \\ \delta \mathbf{x}_1 \\ \vdots \\ \delta \mathbf{x}_K \end{pmatrix} \quad \underline{\mathbf{B}} = \underline{\tilde{\mathbf{B}}}^e = \begin{pmatrix} \tilde{\mathbf{B}}_{0,0}^e & \tilde{\mathbf{B}}_{0,1}^e & \cdots & \tilde{\mathbf{B}}_{0,K}^e \\ \tilde{\mathbf{B}}_{1,0}^e & \tilde{\mathbf{B}}_{1,1}^e & & \tilde{\mathbf{B}}_{1,K}^e \\ \vdots & & \ddots & \\ \tilde{\mathbf{B}}_{K,0}^e & \cdots & & \tilde{\mathbf{B}}_{K,K}^e \end{pmatrix} \quad \text{Provided by an EDA}$$

# Towards a 4D scheme

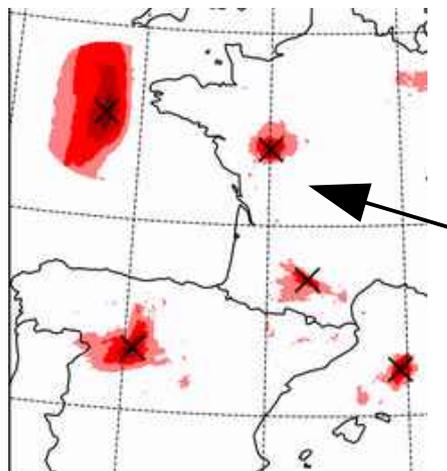
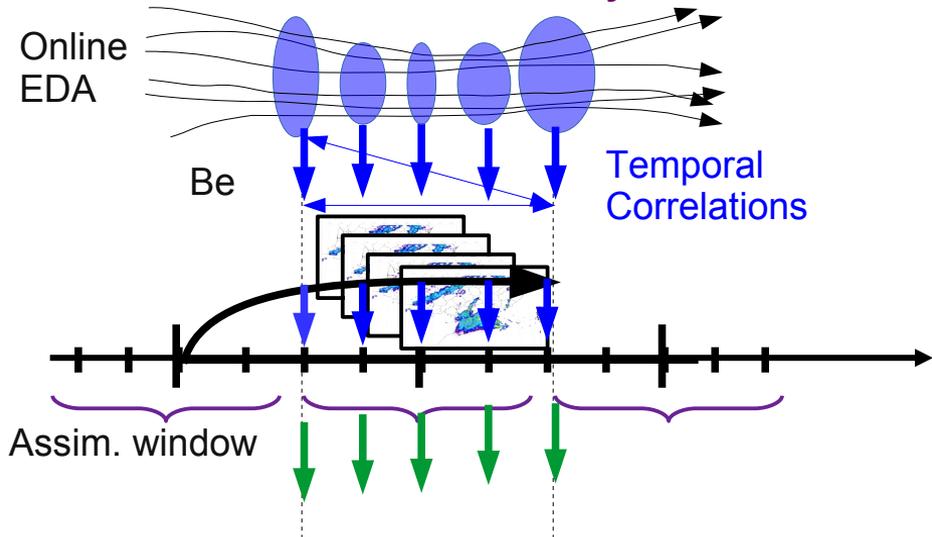
## AROME 4D-Var, 1-h Cycle



Bm :  
-climatological  
-spectral  
-homogenous  
(as in 3dvar)



## AROME 4DEnvar, 1-h Cycle

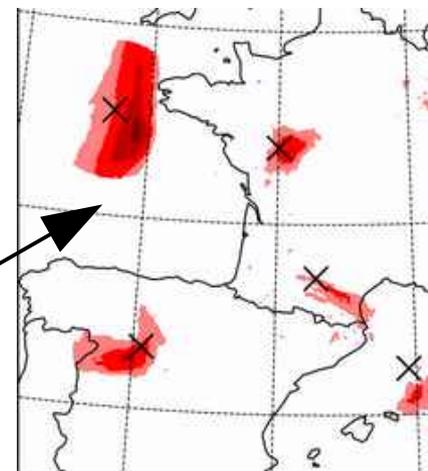


q 850hPa  
error  
correlation

at h-30m

between  
h-30m and  
h+30m

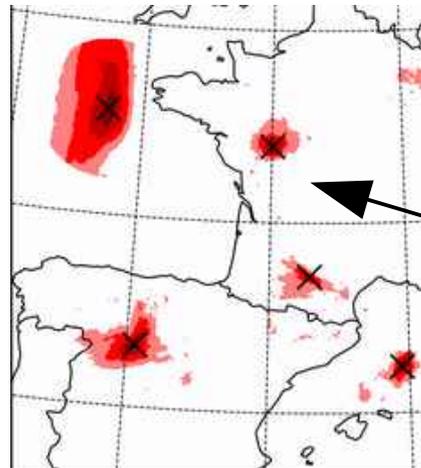
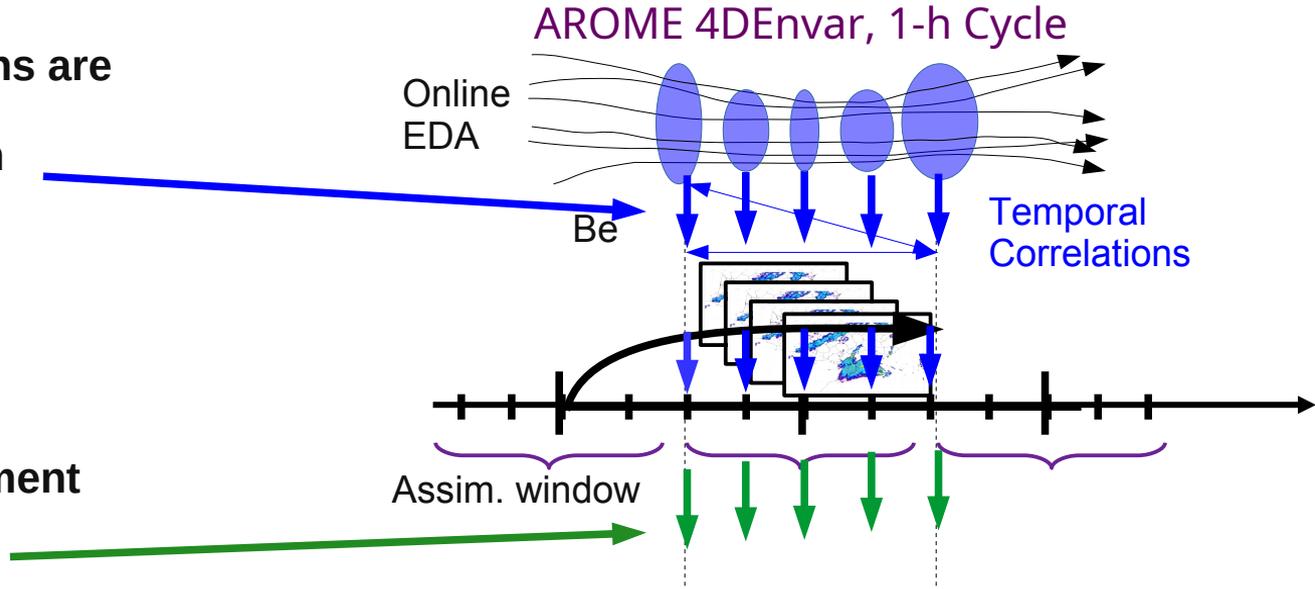
(V. Chabot)



## Towards a 4D scheme : 2 challenges

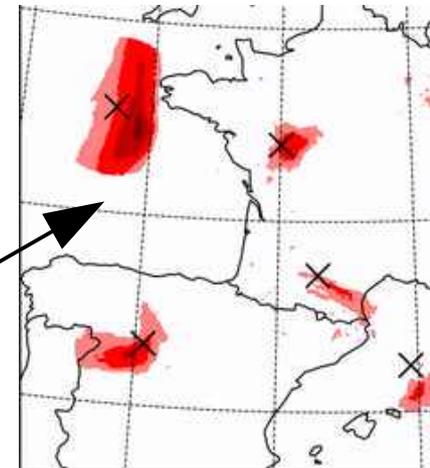
How the temporal error correlations are able to manage the temporal information along the assimilation window ?

How should we use the 4D increment to start the new forecast ?

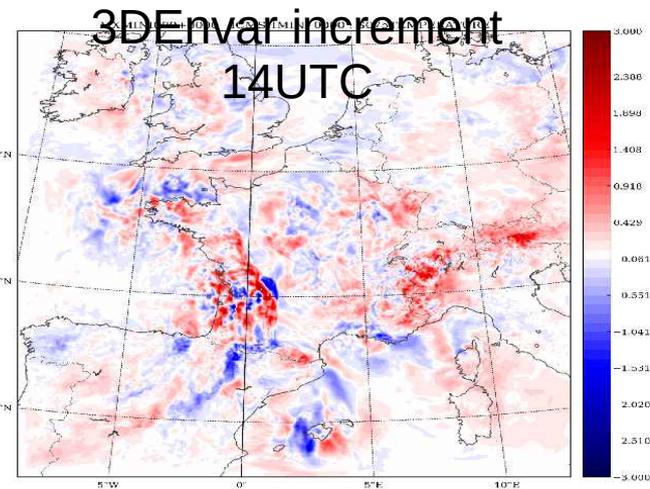
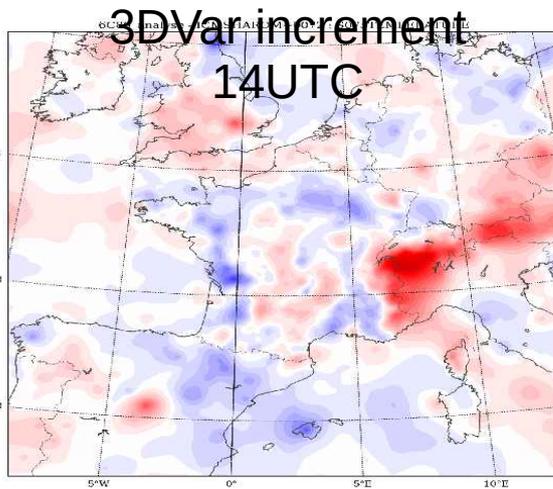
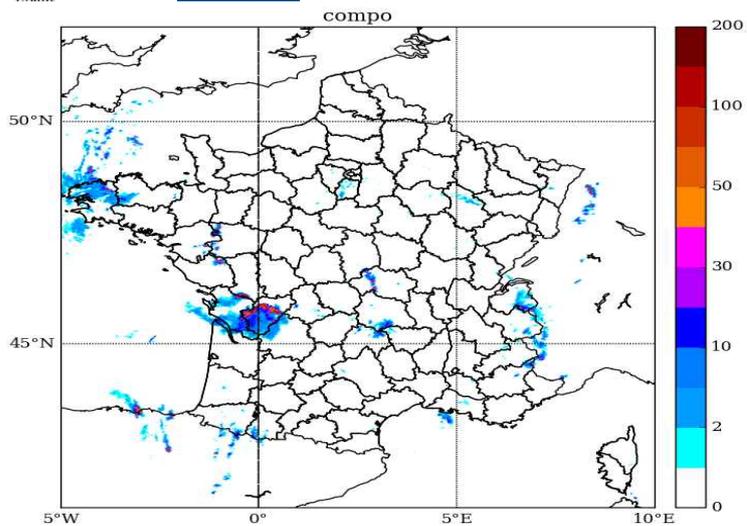


between  
 h-30m and  
 h+30m

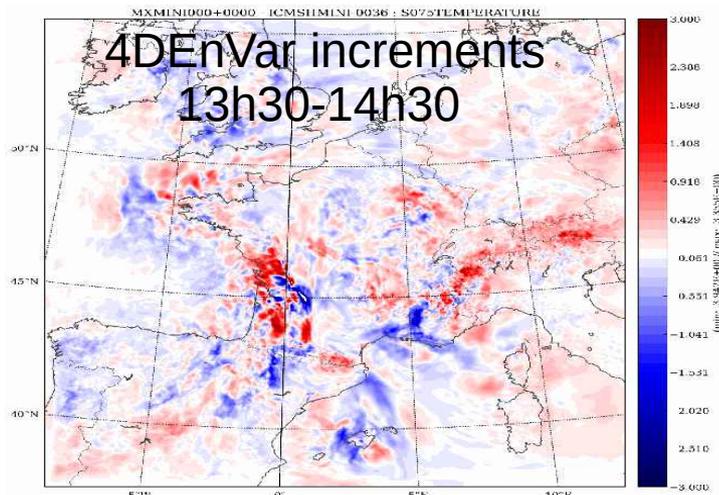
(V. Chabot)



# 4D Temperature increment at 850 hPa



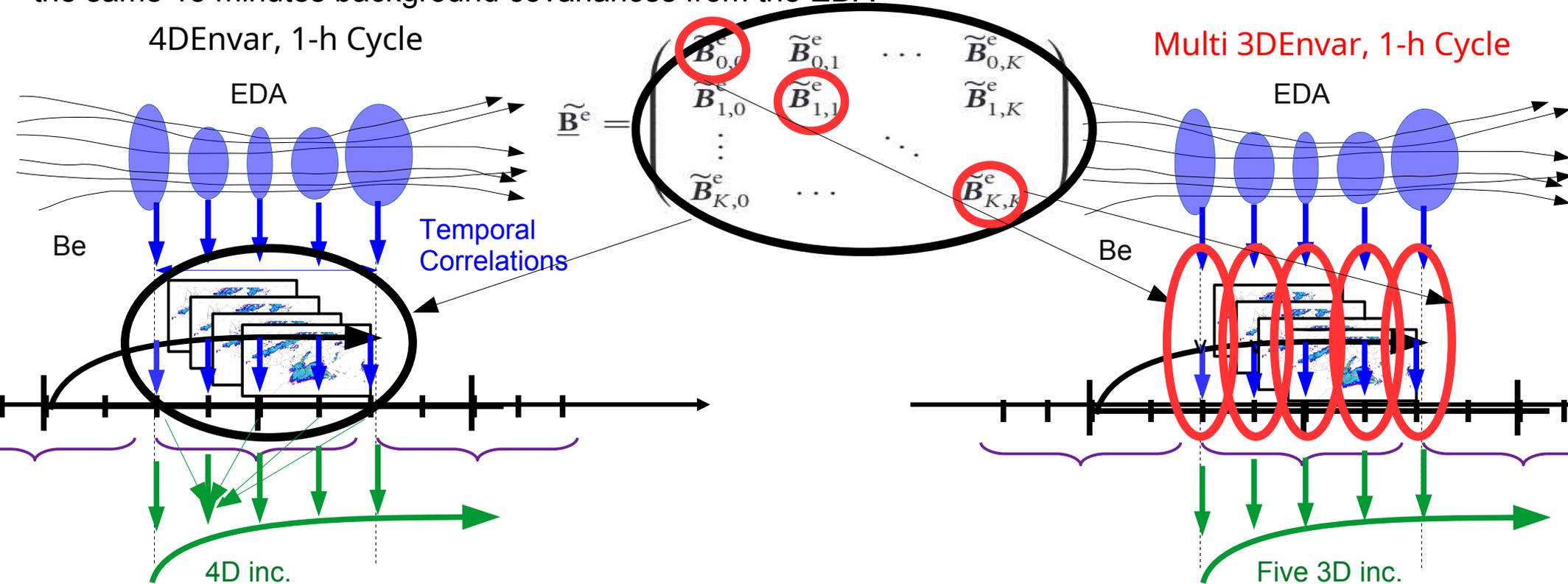
Using the same radar observations  
only at the assimilation window center



# Temporal correlation highlight

One 4DEnVar minim compared to five 3DEnVar minims using :

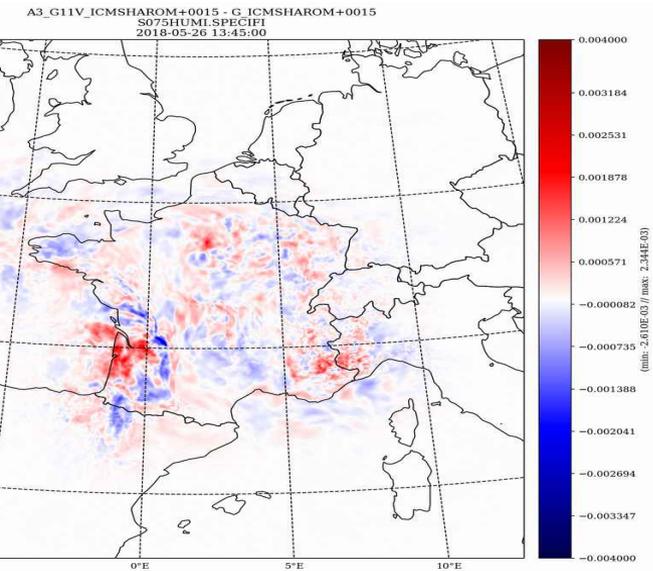
- the same observations : only 15 minutes radar
- the same 15 min background states
- the same 15 minutes background covariances from the EDA



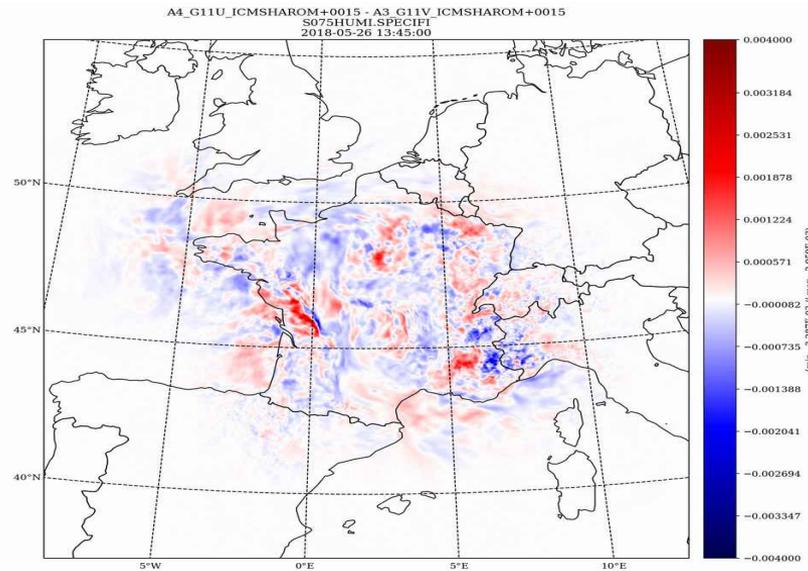
# Temporal correlation highlight

15 min animation of the specific humidity analysis increment at 850 hPa : 14 UTC

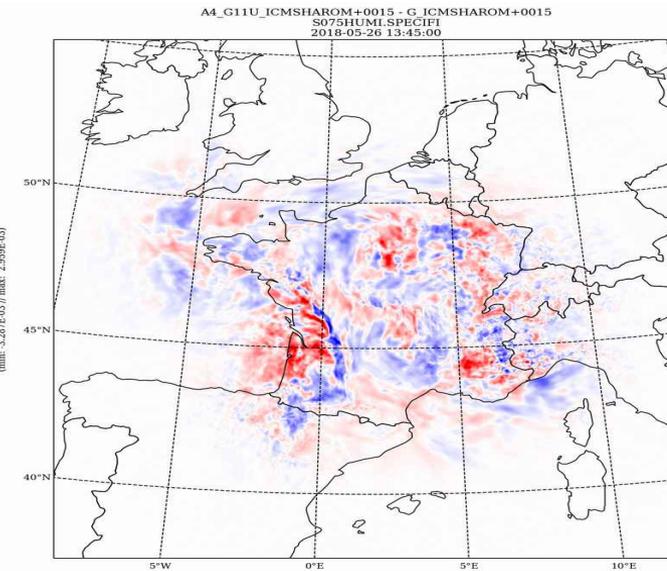
Multi 3DEnvar



4DEnvar-M3DEnvar



4DEnvar



- increment and differences of the same magnitude
- 4DEnVar increment as a better temporal consistency

# Temporal correlation of the increment

Temperature at 850 hPa

Multi 3D $\text{Envar}$

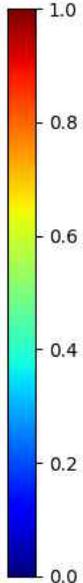
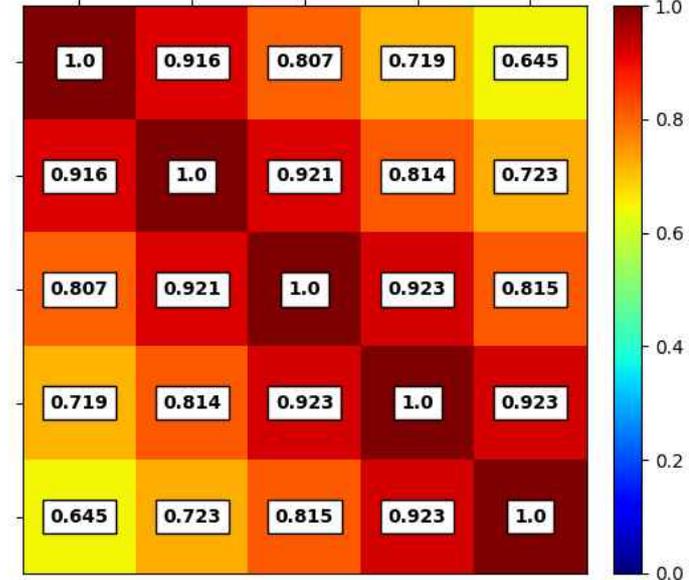
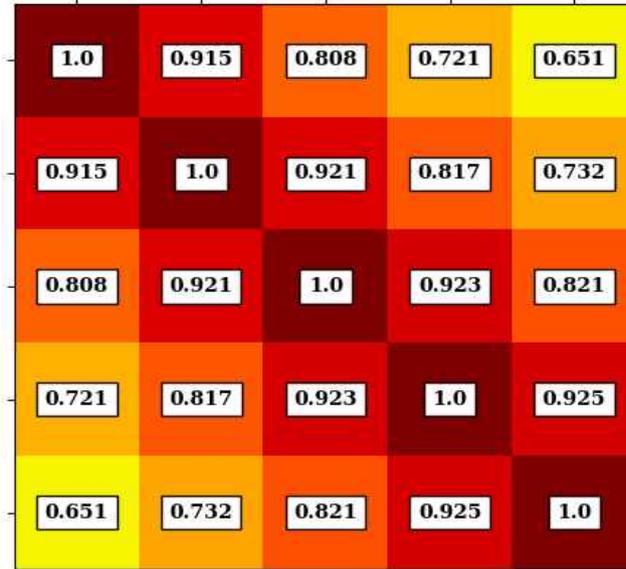
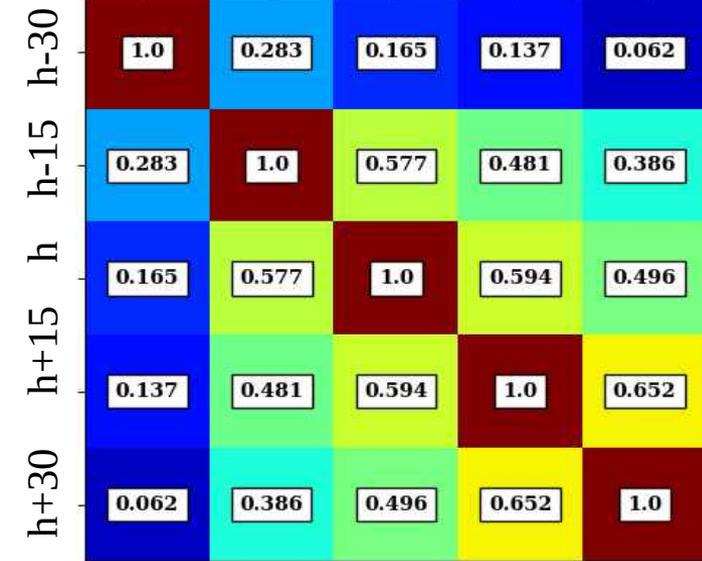
4D $\text{Envar}$  obs 15min

4D $\text{Envar}$  obs 1h

h-30 h-15 h h+15 h+30

t0 t1 t2 t3 t4

t0 t1 t2 t3 t4



- Non diagonal correlations higher in 4D $\text{Envar}$  ( $\sim \times 2$ )
- the correlation between the farthest timeslots in 4D $\text{Envar}$  is higher than between the nearest ones in Multi 3D $\text{Envar}$

# outlines

- **Introduction to a 4DEnVar DA system**
- **Proposal for the next AROME-France E-suite and evaluation.**

# Implementation

\* Based on the current 3DEnVar implementation :

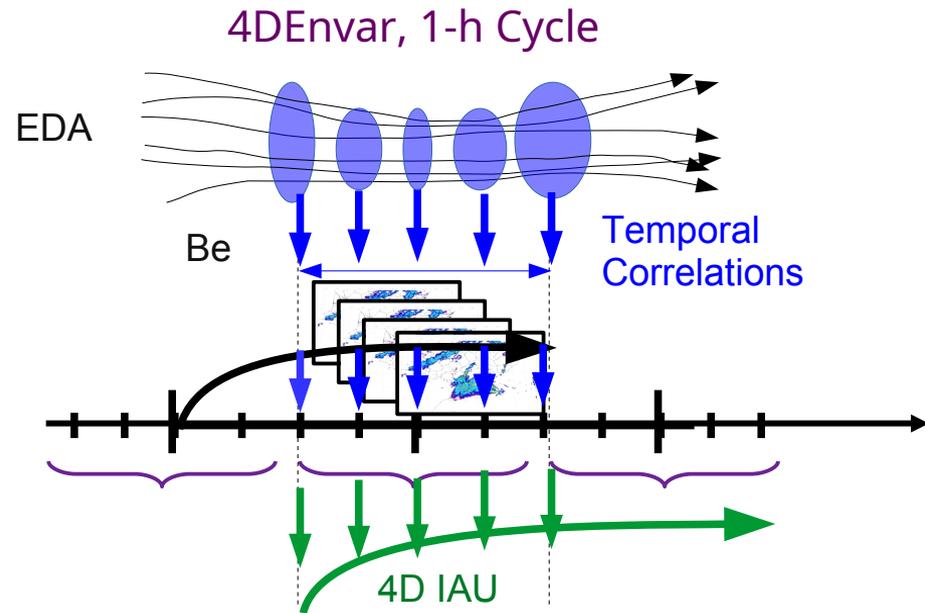
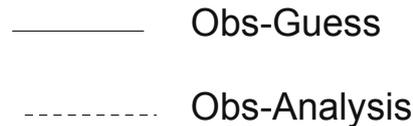
- 1,3km horizontal resolution
- 1 hr assimilation window with 5 timeslots (2x 7 min + 3x 15 min)
- same observations but radar, SEVIRI, ground-based GNSS and surface stations every 15min
- perturbations from a 50 members EDA (3DVar in 3hr cycle at 3,2km ) at each timeslot : every 15min
- Localisation length : 25 km at the lowest level to 150km at the highest one

\* Challenge : how to use the 4D increment ? In theory, all 3D states are statistically equivalent, and the new forecast can be initiated from any of them :

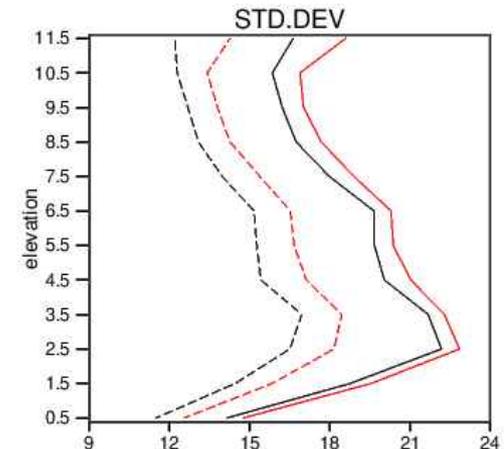
- the first one (as in 4D-Var) ?
- the central one (as in 3D-Var or 3DEnvar) ?
- actually, better results are obtained by using 20% of all of them by 4D IAU

4D IAU (20 % of the 5 Inc.)

3D IAU of the Central Inc. (as in 3DEnVar)



RADAR Globe  
Used RH



## Numerical cost

\* Numerical cost Vs 3DEnVar :

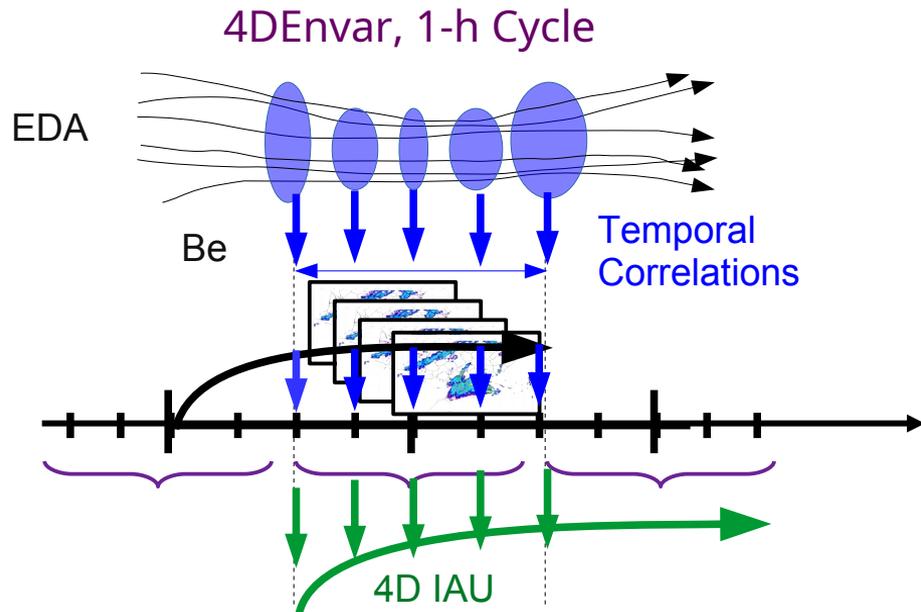
- screening+minim : time x 2, memory x 5 :

=> need for 24 MF's HPC nodes to run screening+minim in 12 min (12 nodes for 3DEnvar in 10 min or 34 nodes to run a 24h arome forecast in 30 min).

- due to the use of 4D IAU : time x 2 due to the forecast to produce the next background : need for a 2 hr forecast range instead of 1 hr

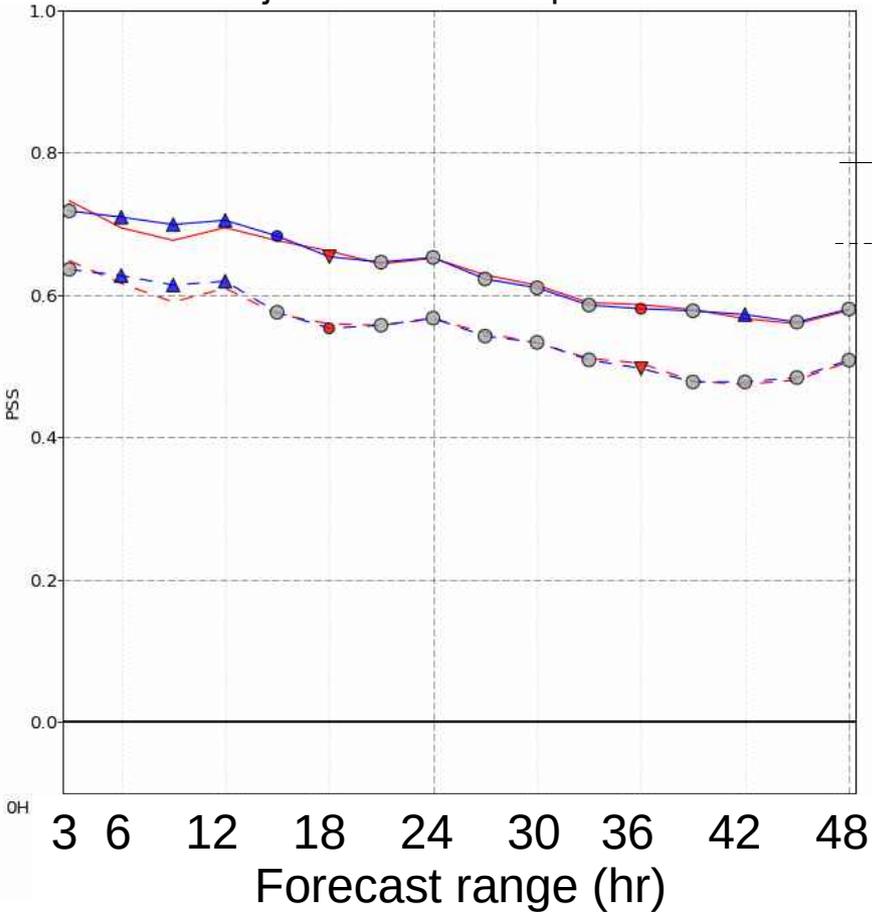
=> +5min on the current 12 nodes used for the DA background

**All these additional numerical costs are affordable on the current MF's HPC**

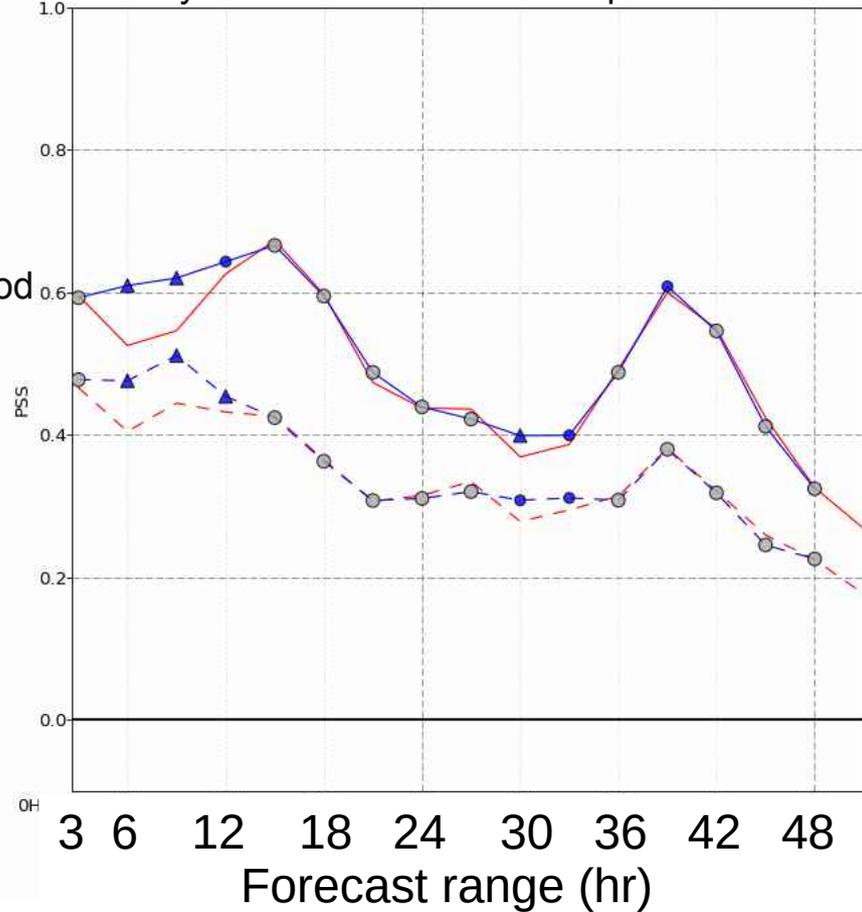


# Long range forecast performances (00 UTC) : PSS for RR3h against raingauges : 2mm/3h threshold (but representative of other thresholds)

Oct 2023 – jan 2024 : winter period



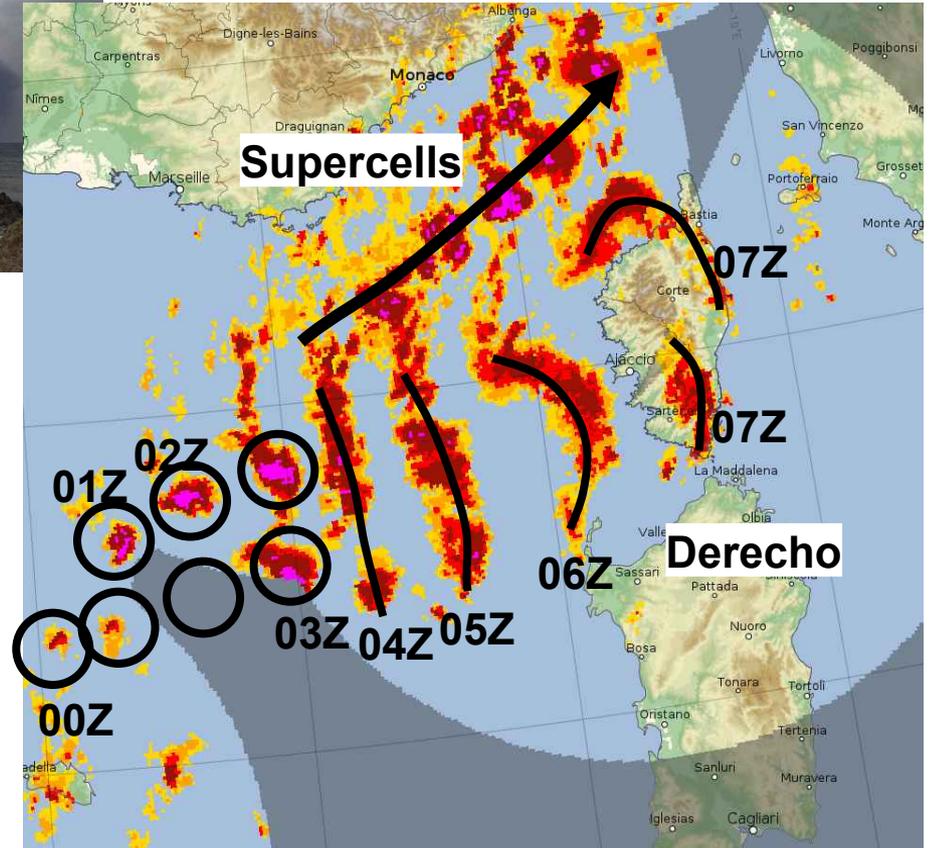
May - Jun 2023 : convective period



## Case study : derecho over Corsica 18 Aug. 2022



- 100-120 km/h generalized wind gusts
- 200-225km/h maximal wind gusts
- 5 casualties
- only an late orange warning !!

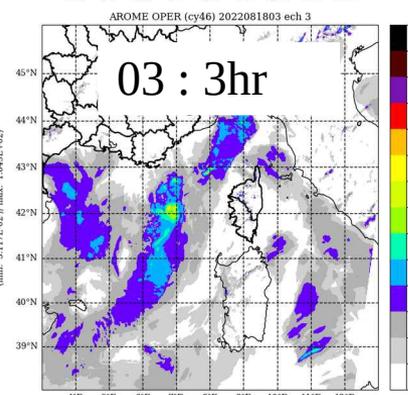
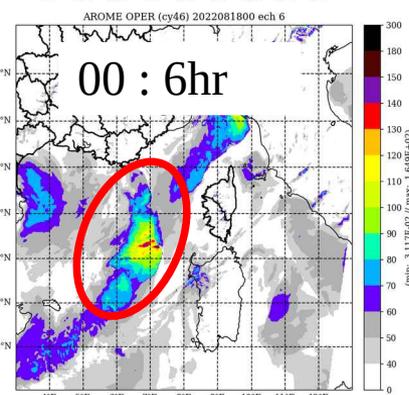
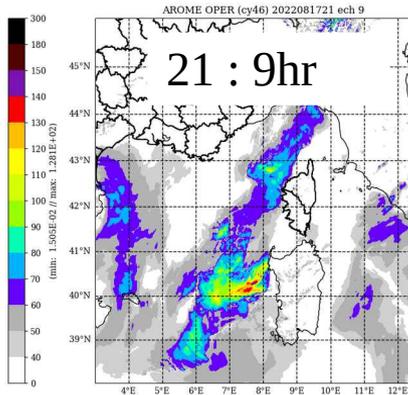
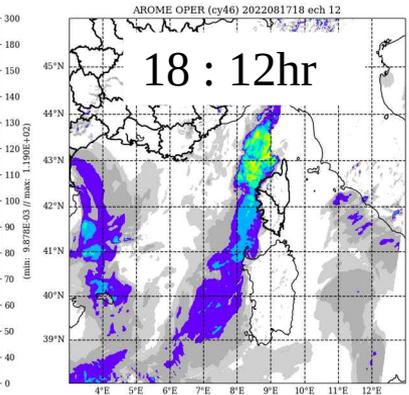
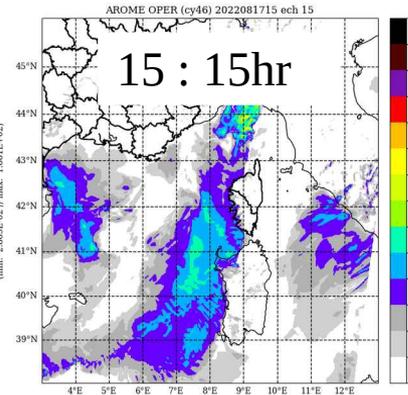
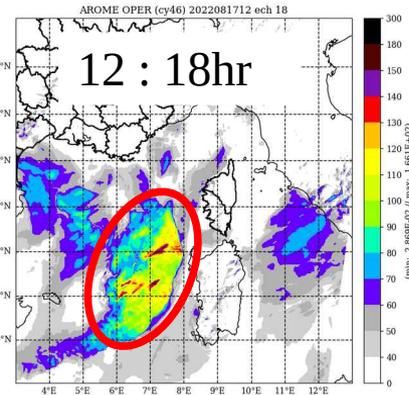
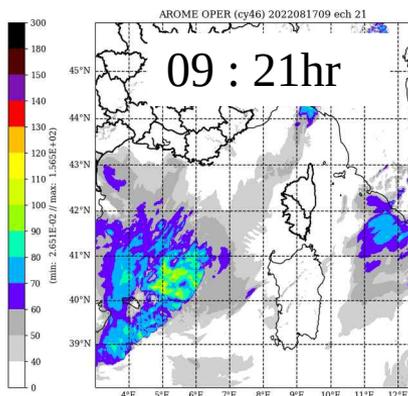
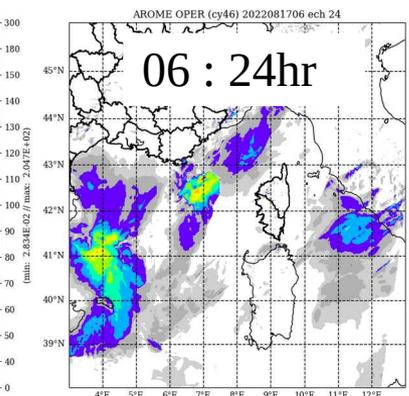
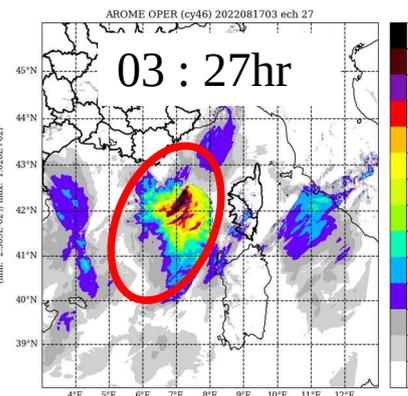
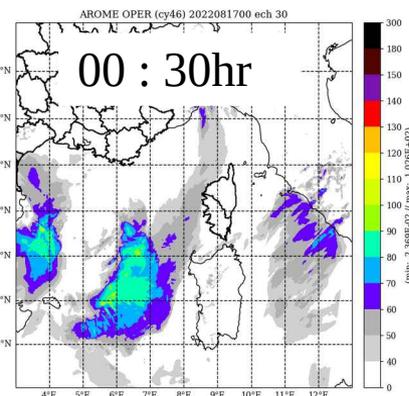


# 3D-Var

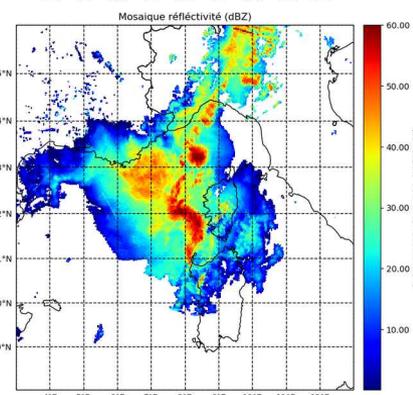
20220817

Wind gusts simulated by the different Arome-france forecasts valid at 06 UTC the 20220818 using 3D-Var : 3 forecasts simulate an interesting signal (Yellow > 110 Km/h)

20220818



Radar reflectivities  
 Observed at 06 UTC the 20220818

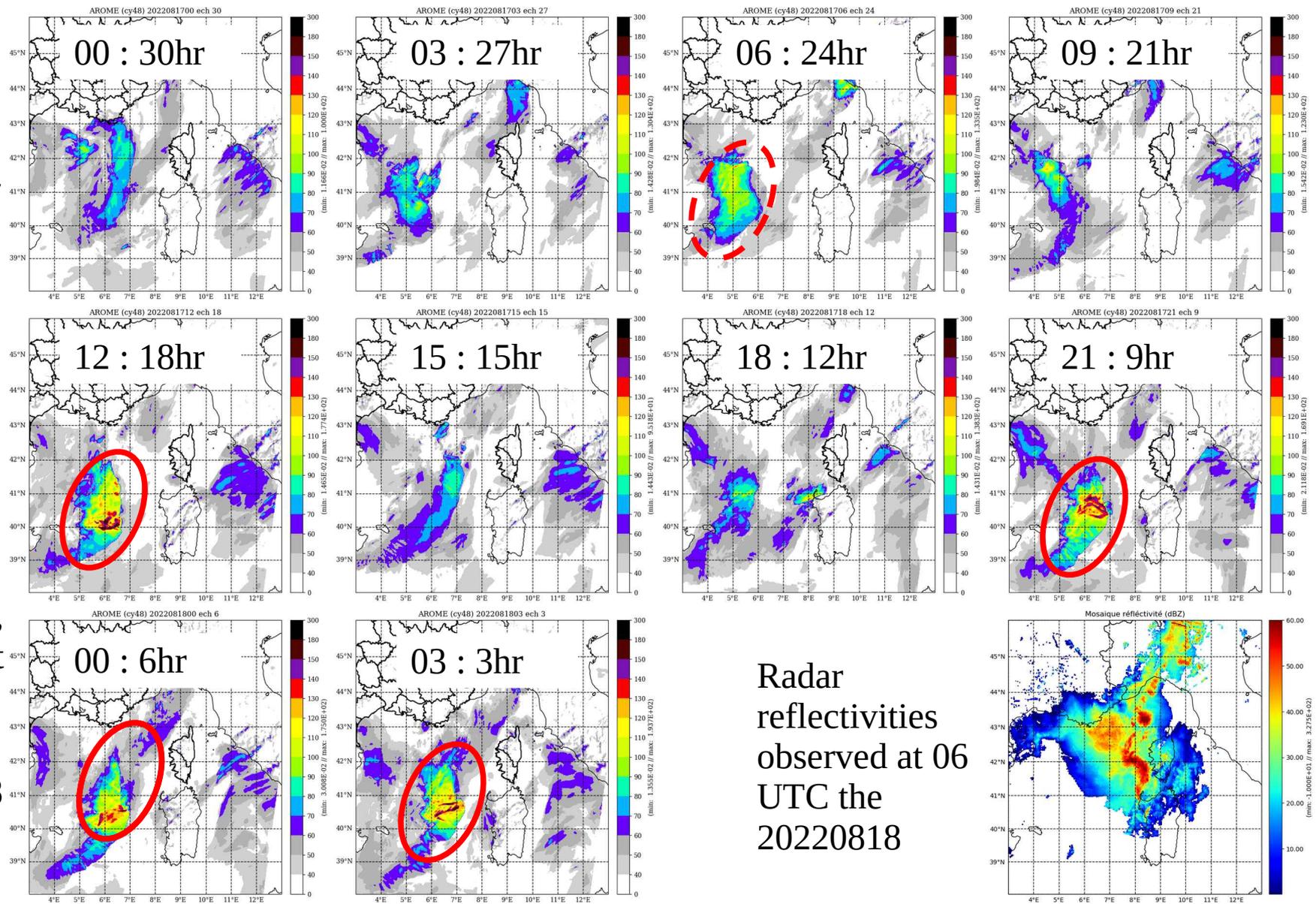


# 3DEnVar

20220817

Wind gusts simulated by the different Arome-france forecasts valid at 06 UTC the 20220818 using 3DEnVar : 5 forecasts simulate an interesting signal, especially the last 3 ones (Yellow > 110 Km/h)

20220818



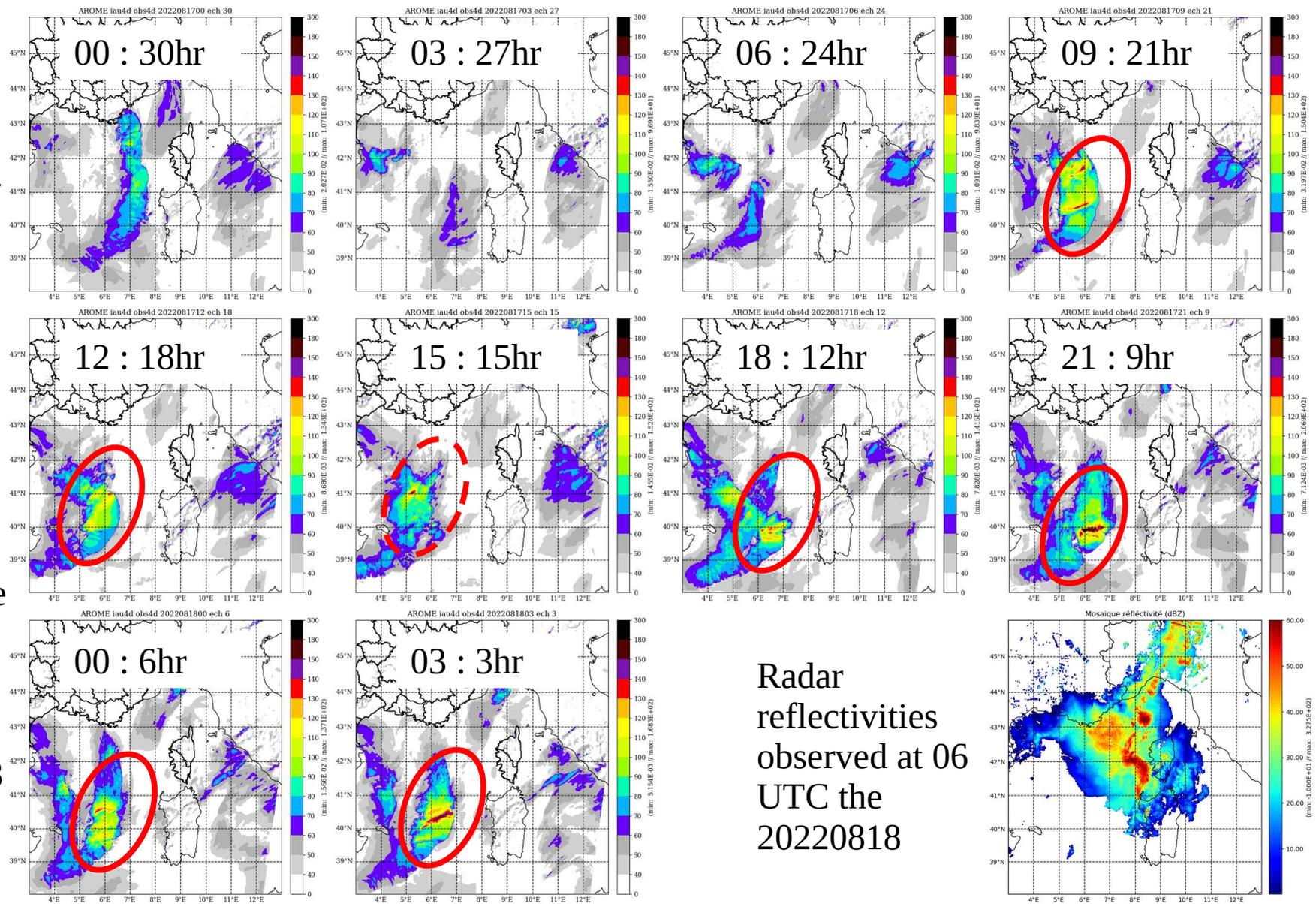
Radar reflectivities observed at 06 UTC the 20220818

# 4DEnVar

20220817

Wind gusts simulated by the different Arome-france forecasts valid at 06 UTC the 20220818 using 4DEnVar : the last 7 forecasts simulate an interesting signal (Yellow > 110 Km/h)

20220818



Radar reflectivities observed at 06 UTC the 20220818

## Conclusion

A 4DEnVar scheme, utilising OOPS, has reached a sufficient level of maturity and has been well evaluated within the Arome-France framework :

- The temporal dimension is managed by the temporal background error cross-correlations, which are directly estimated from the AROME-France EDA (perturbed non-linear model forecasts)
- This allows for the assimilation of 15-min frequency observations in the 1 hr cycle
- Screening + minim run in 12 min on 24 MF's HPC nodes which is affordable operationally
- General performances (classical scores) are comparable to those of 3DEnVar, but precipitation scores (especially during convective periods) and the simulation of severe events have been improved.
- This 4DEnVar configuration is proposed for incorporation in the next MF E-suite, in addition to Scale Dependent Localisation (V. Vogt) and direct assimilation of radar reflectivities (M. Martet).

Thank you for your attention ...

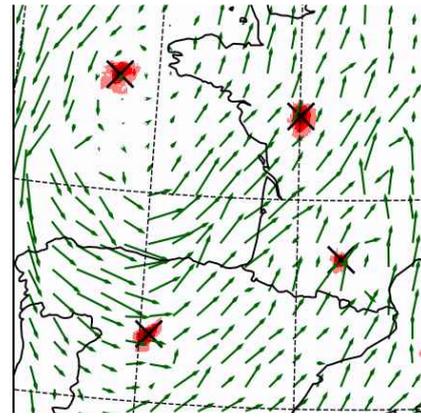
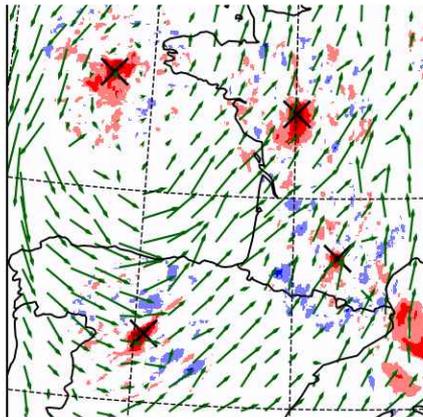
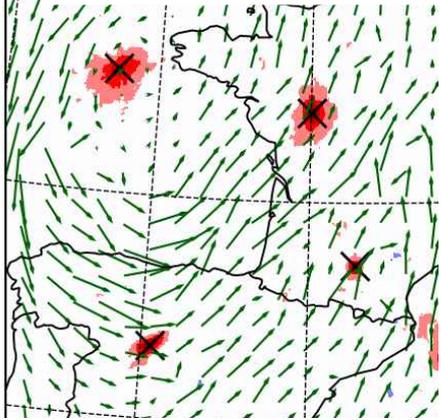
# Horizontal temporal correlation : Specific humidity at 850 hPa

T+0 : auto-correlations

200 members

50 members

50 members + Loc 66km

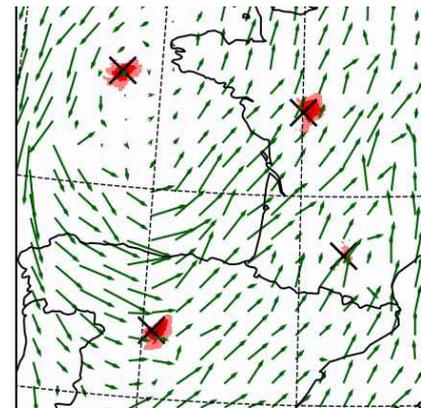
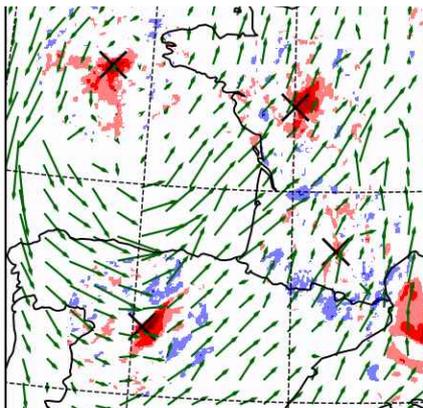
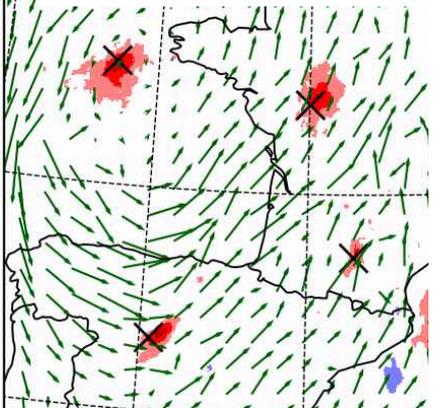


T+60min : 1hr temporal correlations

200 members

50 members

50 members + Loc 66km



# Assimilation cycle statistics : (obs-guess) and (obs-analysis) 20231016-20231216

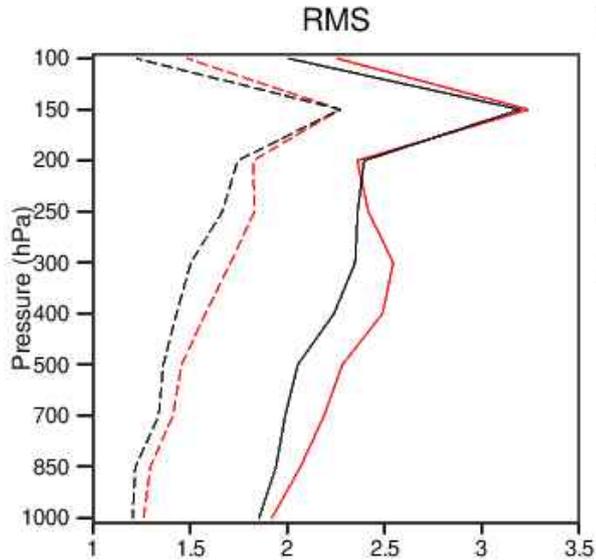
MODES wind :

- more consistent obs-guess comparison
- ~ obs number (+ 4 %)
- and reduced obs-guess and obs-analysis

Radar HU :

- obs number x 4
- reduced obs-guess and obs-ana

MODES-Vwind N.Hemis  
Used V

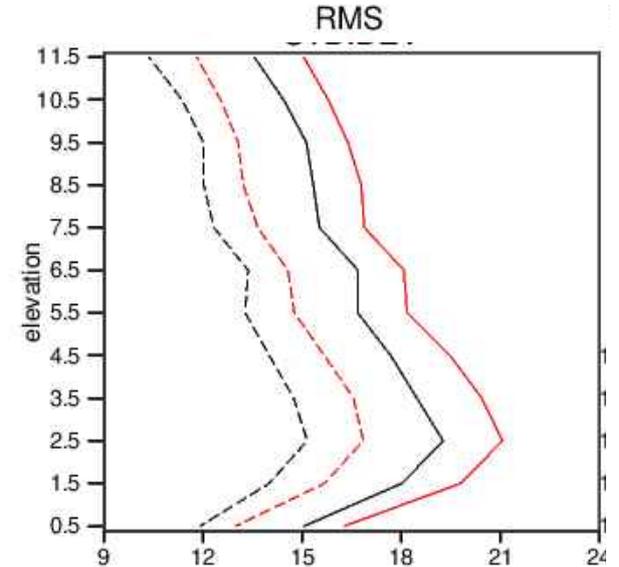


4DEnVar

3DEnVar

- Obs-Guess
- - - Obs-Analysis

RADAR Globe  
Used RH



# 3DEnVar => 4DEnVar + 4DIAU + 4DOBS

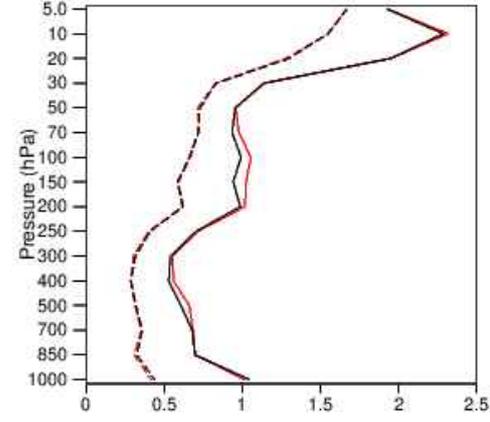
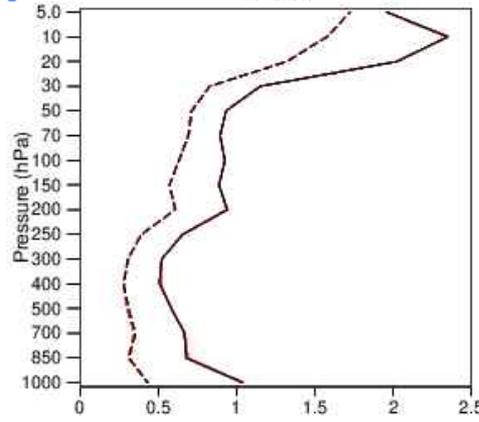
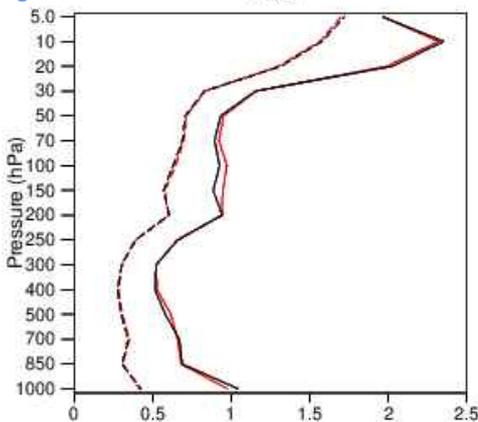
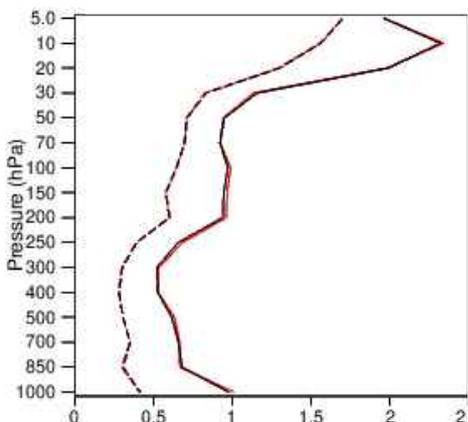
TEMP-T  
Used T

4DEnvar Vs 3DEnvar  
IAU and Obs as  
in 3DEnvar

4DEnvar Vs 4DENVar  
+ 4DIAU + 3DIAU

4DEnvar Vs 4DENVar  
+ 4DIAU + 4DOBS  
+ 4DOBS 3DOBS

4DEnvar Vs 3DENVar  
+ 4DIAU  
+ 4DOBS RMS



RADAR Globe  
Used RH

Obs-Guess

Obs-Analysis

